# Analysis of fuzzy cognitive maps in prediction of individual household electric power consumption

Aleksander Jastriebow\*,\*\*\*, Katarzyna Piotrowska\*

\*Kielce University of Technology

\*\*Kazimierz Pulaski University of Technology and Humanities in Radom

Abstract: This paper is devoted to the simulation analysis of application of a fuzzy cognitive map (FCM) in prediction of electric power consumption by an individual household. Fuzzy cognitive maps and multi-step supervised learning based on gradient method and real data were described. Model of the system for prediction of individual household electric power consumption was implemented on prepared software tool ISEMK (intelligent expert system based on cognitive maps). Simulation research of multi-step learning and testing of FCM were done based on real data. Chosen results of simulation were presented.

**Keywords:** fuzzy cognitive maps, prediction system, multi-step supervised learning, gradient method

Modeling of prediction systems can be done by developing a model based on selecting crucial concepts for the analyzed issue and defining the relations between them. Model of this type is called a fuzzy cognitive map (FCM) [11]. This paper is devoted to the analysis of FCM in prediction of individual household electric power consumption.

### 1. Introduction

Fuzzy cognitive map is a directed graph, whose nodes denote concepts relevant to the analyzed issue. The concepts influence each other with the intensity described by the relation weight between them [17].

FCM is widely used in decision support systems, e.g. in socio-economic models [9], in logistics [8], in supplier selection [19], in road transport [13], in intrusion detection [16] and medical expert systems [1, 4, 10, 12]. Fuzzy cognitive maps are especially popular in prediction systems, for example, in stock market decision support system [2], in predicting autistic disorder [10] and pulmonary infection [12], in numerical and linguistic prediction of time series [18].

This paper presents system for prediction of individual household electric power consumption based on fuzzy cognitive map. Part 2 describes the structure and dynamic model of FCM. In part 3 multi-step algorithm of supervised learning based on gradient method and real data is presented. Part 4 briefly characterizes the prepared soft-

ware tool ISEMK (intelligent expert system based on cognitive maps), enabling the modeling of prediction systems. Part 5 describes system for prediction of individual household electric power consumption and contains chosen results of simulation research of learning and testing the system, done in ISEMK. Part 6 contains a summary of the work.

## 2. Fuzzy cognitive maps

The basis of the structure of FCM is a directed graph in the form [17]:

$$\langle X, R \rangle$$
 (1)

where  $X=[X_1,...,X_n]^T$  – the set of the concepts, n – the number of concepts;  $R=\{r_{j,i}\}$  – relations' matrix,  $r_{j,i}$  – the relation weight between the concept j and the concept i (value from the range [-1, 1]).

Dynamic models of FCM were presented in [5]. In this paper a nonlinear dynamic model described by the following equation was used:

$$X_{i}(t+1) = F \left( X_{i}(t) + \sum_{\substack{j=1\\j \neq i}}^{n} r_{j,i} \cdot X_{j}(t) \right)$$
 (2)

where: t – discrete time, t=0,1,2,...,T, T – end time of simulation;  $X_i(t)$  – the value of the i concept (value from the range [0,1]), i=1,2,...,n; F(x) – sigmoid stabilizing function

FCM as an intelligent system has the ability of learning of relations' matrix based on real data. Below the idea of multi-step supervised learning of FCM was presented.

### 3. Multi-step supervised learning

Characteristic feature of multi-step supervised learning of FCM is the estimation of a current value of the relations' matrix element on the basis of a few previous estimations, which can be achieved as follows [6, 7]:

$$r_{j,i}(t+1) = P_{[-1,1]} \left( \sum_{k=0}^{m_1} \alpha_k \cdot r_{j,i}(t-k) + \sum_{l=0}^{m_2} \beta_l \cdot \eta_l(t) \cdot \Delta J_{j,i}(t-l) \right)$$
(3)

where:  $\alpha_k$ ,  $\beta_l$ ,  $\eta_l$  – learning parameters  $(k=1,...,m_1; l=1,...,m_2)$ ;  $m_1$ ,  $m_2$  – the number of the steps of the algorithm;  $\Delta J_{j,i}(t)$  – gradient of error function;  $P_{[-1,1]}(x)$  – operator design for the set [-1,1], described by the equation:

$$P_{[-1,1]}(x) = \begin{cases} -1 & for & x \le -1 \\ x & for & -1 < x < 1 \\ 1 & for & x \ge 1 \end{cases}$$
 (4)

A special case of algorithm (3) is the known neural network learning algorithm (i.e. back propagation algorithm with the moment). Multi-step algorithms are some kind of generalization of known one-step methods of learning. Below multi-step supervised learning based on gradient method and real data was described.

### 3.1. Gradient method

Supervised learning based on gradient method is a modification of the weights in the direction of steepest descent of error function described by the equation [7]:

$$J(t) = \frac{1}{n} \sum_{i=1}^{n} (X_i(t) - Z_i(t))^2$$
 (5)

where:  $Z_i(t)$  – the reference value of the *i* concept.

Reference values can be obtained through normalization of the real data as follows:

$$f(x) = \frac{x - \min}{\max - \min} \tag{6}$$

where: x – input numeric value; min – the minimum of the dataset, max – the maximum of the dataset.

Gradient of error function for the gradient method (3) is described with the equation [5]:

$$\Delta J_{i,i}(t) = (Z_i(t) - X_i(t)) \cdot y_{i,i}(t) \tag{7}$$

where:  $y_{j,i}(t)$  – sensitivity function described as follows:

$$y_{j,i}(t+1) = (y_{j,i}(t) + X_j(t)) \cdot F'(X_i(t) + \sum_{\substack{j=1\\i\neq j}}^n X_j(t) \cdot r_{j,i}(t))$$

$$(8)$$

where: F'(x) – derivative of stabilizing function.

Learning parameters  $\alpha_k$ ,  $\beta_l$ ,  $\eta_l$  must satisfy conditions (9)–(12) to obtain the convergence of multi-step learning algorithm [6]:

$$\sum_{k=0}^{m_1} \alpha_k = 1 \tag{9}$$

$$0 < \eta_l(t) < 1 \tag{10}$$

$$\eta_l(t) = \frac{1}{\lambda_l + t} \tag{11}$$

$$\beta_l \ge 0 \tag{12}$$

A special case of multi-step supervised learning is onestep gradient method, which consists in modifying the relations' matrix according to the formula:

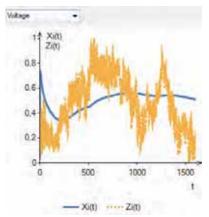
$$r_{j,i}(t+1) = P_{[-1,1]} \left( r_{j,i}(t) + \beta \cdot \eta(t) \cdot \Delta J_{j,i}(t) \right)$$
 (13)

Simulation analysis of the multi-step supervised learning was realized based on ISEMK system. Below basic functionality of ISEMK was presented.

### 4. ISEMK system

Intelligent expert system based on cognitive maps ISEMK [14, 15] is a software tool for modeling decision support systems using FCM. The application was developed using the Visual Studio by Microsoft. ISEMK enables:

- the construction of FCM,
- the initialization of values of relations' matrix and map concepts based on expert knowledge or real data,
- reading and writing of FCM parameters using .xml files,
- dynamic monitoring of FCM,
- multi-step supervised and unsupervised learning of FCM.
- the analysis of designed learned FCM by testing system operation based on real data,
- exporting data of learning and FCM analysis to .xls files,
- proper visualizations of done research on devised computer software.

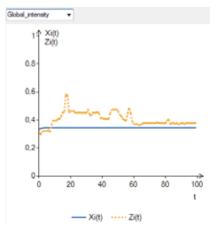


**Fig. 1.** Visualization of multi-step supervised learning results in the ISEMK system

**Rys. 1.** Wizualizacja wyników wielokrokowego uczenia nadzorowanego w systemie ISEMK

Fig. 1 shows an exemplary visualization of multi-step supervised learning results in the ISEMK system.

Fig. 2 shows an exemplary visualization of testing of the learned FCM operation in the ISEMK system.



**Fig. 2.** Visualization of testing of learned FCM operation in the ISEMK system

Rys. 2. Wizualizacja testowania działania nauczonej FCM w systemie ISEMK

# Simulation analysis of fuzzy cognitive maps

Application of FCM was analyzed on the example of prediction of individual household electric power consumption. Below the system of prediction and chosen results of simulation analysis were presented.

### 5.1. System of prediction of individual household electric power consumption

The aim of the modeled system is prediction of individual household electric power consumption. Initialization, multi-step supervised learning and testing of the FCM were realized in ISEMK based on real data taken from Machine Learning Repository [3]. The dataset contains the measurements of electric power consumption obtained within 47 months. On the basis of normalized numerical data, the fuzzy cognitive map with the following concepts was implemented:

 $X_1$  – global\_active\_power: household global minute-averaged active power (in kilowatt),

 $X_2$  – global\_reactive\_power: household global minute-averaged reactive power (in kilowatt),

X<sub>3</sub> – voltage: minute-averaged voltage (in volt),

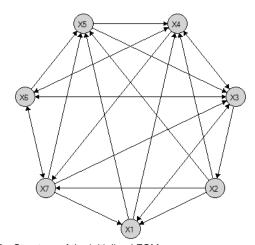
 $X_4$  – global\_intensity: household global minute-averaged current intensity (in ampere),

 $X_5$  – sub\_metering\_1: energy sub-metering No. 1 (in watt-hour of active energy),

 $X_6$  – sub\_metering\_2: energy sub-metering No. 2 (in watt-hour of active energy),

 $X_7 - \text{sub\_metering\_3}$ : energy sub-metering No. 3 (in watt-hour of active energy).

The relations' matrix was initialized with random values from the interval [-0.2, 0.2]. Fig. 3 presents the structure of the initialized FCM.



**Fig. 3.** Structure of the initialized FCM **Rys. 3.** Struktura zainicjalizowanej FCM

The initialized FCM was learned using multi-step supervised learning for various parameters based on 1600 records with the measurements of electric power consumption. Another 100 records were used in testing of learned maps operation. Below, chosen results of learning

### 5.2. Chosen results of FCM learning

end testing of the analyzed system were presented.

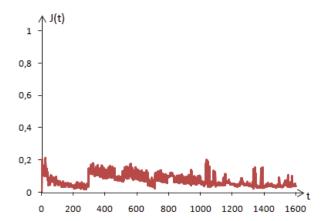
The initialized FCM learned with multi-step gradient method described in part 3. The learning process was realized for the number of steps:  $m_1 \le 2$ ,  $m_2 \le 2$ . Figs. 4–6 show an example of the learning results for the following parameters:  $m_1 = 0$ ,  $m_2 = 2$ ,  $\alpha_0 = 1$ ,  $\alpha_1 = 0$ ,  $\alpha_2 = 0$ ,  $\beta_0 = 5$ ,  $\beta_1 = 3$ ,  $\beta_2 = 2$ ,  $\eta_0(0) = \eta_1(0) = \eta_2(0) = 0.01$ .

Tab. 1. presents the relations' matrix of the FCM learned with the following parameters:  $m_1=1$ ,  $m_2=2$ ,  $\alpha_0=0.7$ ,  $\alpha_1=0.3$ ,  $\alpha_2=0$ ,  $\beta_0=2$ ,  $\beta_1=2$ ,  $\beta_2=1$ ,  $\eta_0(0)=\eta_1(0)=\eta_2(0)=0.1$ .

Tab. 1. Exemplary relations' matrix

Tab. 1. Przykładowa macierz relacji

	$X_1$	$X_2$	$X_3$	$X_4$	$X_5$	$X_6$	$X_7$
$X_1$	0	-0.5	-0.3	-0.3	-0.7	-0.6	0
$X_2$	-0.4	0	-0.4	-0.3	-0.7	-0.6	0.1
$X_3$	-0.3	-0.4	0	-0.4	-0.6	-0.7	0
$X_4$	-0.4	-0.5	-0.3	0	-0.6	-0.7	-0.1
$X_5$	-0.2	-0.2	-0.1	-0.2	0	-0.4	0
$X_6$	-0.2	-0.2	-0.1	-0.1	-0.5	0	0
$X_7$	-0.5	-0.8	-0.3	-0.5	-0.9	-0.8	0



**Fig. 4.** Changes of the error function value during learning **Rys. 4.** Zmiany wartości funkcji błędu w czasie uczenia

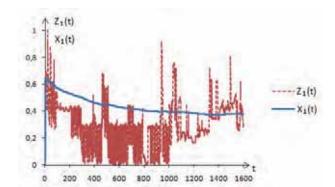


Fig. 5. Changes of the value of the concept  $X_1$  during learning Rys. 5. Zmiany wartości czynnika  $X_1$  w czasie uczenia

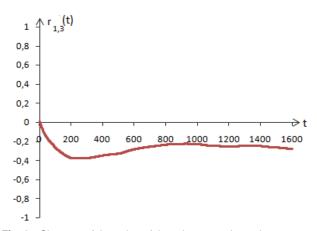


Fig. 6. Changes of the value of the relation  $r_{1,3}$  during learning Rys. 6. Zmiany wartości relacji  $r_{1,3}$  w czasie uczenia

### 5.3. Chosen results of FCM testing

This chapter contains results of the comparative analysis of multi-step algorithms of FCM learning to one-step methods, from the point of view of the obtained average percentage error of prediction for 100 test records, described as follows:

$$J_P = \frac{1}{100} \sum_{t=1601}^{1700} J_P(t) \cdot 100\%$$
 (14)

where:  $J_P(t)$  – prediction error described by the formula:

$$J_P(t) = \frac{1}{n} \sum_{i=1}^{n} (X_i(t) - Z_i(t))^2$$
 (15)

Figs. 7–8 show an example of testing of the operation of FCM, that learned with the following parameters:  $m_1=2, m_2=2, \alpha_0=0.5, \alpha_1=0.3, \alpha_2=0.2, \beta_0=5, \beta_1=3, \beta_2=2, \eta_0(0)=\eta_1(0)=\eta_2(0)=0.01.$ 

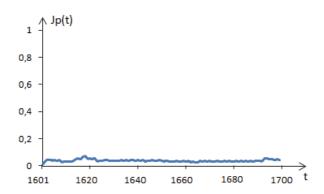


Fig. 7. Changes of the prediction error function value during testing

Rys. 7. Zmiany wartości funkcji błędu predykcji w czasie testowania

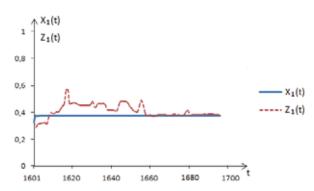


Fig. 8. Changes of the value of the concept  $X_1$  during testing Rys. 8. Zmiany wartości czynnika  $X_1$  w czasie testowania

Tab. 2 presents chosen results of comparative analysis of error  $J_P$  obtained by multi-step learning with error obtained by one-step gradient method for the following parameters:  $m_1$ =0,  $m_2$ =0,  $\alpha_0$ =1,  $\alpha_1$ =0,  $\alpha_2$ =0,  $\beta_0$ =5,  $\beta_1$ =0,  $\beta_2$ =0,  $\eta_0(0)=\eta_1(0)=\eta_2(0)=0.1$  (simulation 1).

Prediction error equal to 3.011 % was obtained as a result of one-step gradient method ( $m_1$ =0,  $m_2$ =0). Increasing the steps number led to reduced average percentage prediction error. The error minimum equal to 2.983 % was obtained for the parameters:  $m_1$ =1,  $m_2$ =2,  $\alpha_0$ =0.7,  $\alpha_1$ =0.3,  $\alpha_2$ =0,  $\beta_0$ =2,  $\beta_1$ =2,  $\beta_2$ =1,  $\eta_0$ (0)= $\eta_1$ (0)= $\eta_2$ (0)=0.1.

Tab. 3 presents chosen results of comparative analysis of error  $J_P$  obtained by multi-step learning with error obtained by one-step gradient method for the following parameters:  $m_1=0$ ,  $m_2=0$ ,  $\alpha_0=1$ ,  $\alpha_1=0$ ,  $\alpha_2=0$ ,  $\beta_0=10$ ,  $\beta_1=0$ ,  $\beta_2=0$ ,  $\eta_0(0)=\eta_1(0)=\eta_2(0)=0.01$  (simulation 2).

**Tab. 2.** Used learning parameters and average percentage error of prediction for the simulation 1

**Tab. 2.** Zastosowane parametry uczenia i średni procentowy bład predykcji dla symulacji 1

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$m_1$	$m_2$	<b>0</b> (0	$\alpha_1$	<b>O</b> 2	$\beta_0$	$\beta_1$	$\beta_2$	$\eta_{0,1,2}(0)$	$J_P[\%]$
0	0	1	0	0	5	0	0	0.1	3.011
0	1	1	0	0	4	1	0	0.1	3.011
0	1	1	0	0	3	2	0	0.1	3.007
0	2	1	0	0	3	1	1	0.1	3.012
0	2	1	0	0	2	2	1	0.1	3.011
1	0	0.8	0.2	0	5	0	0	0.1	2.993
1	0	0.7	0.3	0	5	0	0	0.1	2.985
1	0	0.6	0.4	0	5	0	0	0.1	2.996
2	0	0.7	0.2	0.1	5	0	0	0.1	2.986
1	1	0.7	0.3	0	3	2	0	0.1	2.988
1	2	0.7	0.3	0	2	2	1	0.1	2.983
2	1	0.7	0.2	0.1	3	2	0	0.1	2.989
2	2	0.7	0.2	0.1	2	2	1	0.1	2.986

**Tab. 3.** Used learning parameters and average percentage error of prediction for the simulation 2

**Tab. 3.** Zastosowane parametry uczenia i średni procentowy błąd predykcji dla symulacji 2

$m_1$	$m_2$	<b>0</b> (0	$\alpha_1$	<b>0</b> ⁄2	$\beta_0$	$\beta_1$	$\beta_2$	$\eta_{0,1,2}(0)$	$J_P[\%]$
0	0	1	0	0	10	0	0	0.01	3.793
0	1	1	0	0	8	2	0	0.01	3.792
0	1	1	0	0	6	4	0	0.01	3.789
0	2	1	0	0	6	3	1	0.01	3.789
0	2	1	0	0	5	3	2	0.01	3.789
1	0	0.8	0.2	0	10	0	0	0.01	3.734
1	0	0.6	0.4	0	10	0	0	0.01	3.714
2	0	0.6	0.3	0.1	10	0	0	0.01	3.713
2	0	0.5	0.3	0.2	10	0	0	0.01	3.711
2	1	0.5	0.3	0.2	6	4	0	0.01	3.707
1	2	0.6	0.4	0	5	3	2	0.01	3.711
2	2	0.5	0.3	0.2	5	3	2	0.01	3.707
0	0	1	0	0	10	0	0	0.01	3.793

**Tab. 4.** Used learning parameters and average percentage error of prediction for the simulation 3

**Tab. 4.** Zastosowane parametry uczenia i średni procentowy błąd predykcji dla symulacji 3

$m_1$	$m_2$	<b>O</b> (0	$\alpha_1$	<b>O</b> 2	$\beta_0$	$\beta_1$	$\beta_2$	$\eta_{0,1,2}(0)$	$J_P[\%]$
0	0	1	0	0	10	0	0	0.1	3.348
0	1	1	0	0	8	2	0	0.1	3.345
0	1	1	0	0	6	4	0	0.1	3.318
0	2	1	0	0	5	3	2	0.1	3.324
0	2	1	0	0	7	2	1	0.1	3.337
1	0	0.8	0.2	0	10	0	0	0.1	3.267
1	0	0.6	0.4	0	10	0	0	0.1	3.191
2	0	0.5	0.3	0.2	10	0	0	0.1	3.161
2	1	0.5	0.3	0.2	6	4	0	0.1	3.167
1	2	0.6	0.4	0	5	3	2	0.1	3.193
1	1	0.6	0.4	0	6	4	0	0.1	3.187
2	2	0.5	0.3	0.2	5	3	2	0.1	3.154
0	0	1	0	0	10	0	0	0.1	3.348

Prediction error equal to 3.793 % was obtained as a result of one-step gradient method ( $m_1$ =0,  $m_2$ =0). In-

creasing the steps number led to reduced average percentage prediction error. The error minimum equal to 3.707 % was obtained for the following parameters:  $m_1=2$ ,  $m_2=1$ ,  $\alpha_0=0.5$ ,  $\alpha_1=0.3$ ,  $\alpha_2=0.2$ ,  $\beta_0=6$ ,  $\beta_1=4$ ,  $\beta_2=0$ ,  $\eta_0(0)=\eta_1(0)=\eta_2(0)=0.01$  and  $m_1=2$ ,  $m_2=2$ ,  $\alpha_0=0.5$ ,  $\alpha_1=0.3$ ,  $\alpha_2=0.2$ ,  $\beta_0=5$ ,  $\beta_1=3$ ,  $\beta_2=2$ ,  $\eta_0(0)=\eta_1(0)=\eta_2(0)=0.01$ .

Tab. 4 presents chosen results of comparative analysis of error  $J_P$  obtained by multi-step learning with error obtained by one-step gradient method for the parameters:  $m_1=0, m_2=0, \alpha_0=1, \alpha_1=0, \alpha_2=0, \beta_0=10, \beta_1=0, \beta_2=0, \eta_0(0)=\eta_1(0)=\eta_2(0)=0.1$  (simulation 3).

Prediction error equal to 3.348 % was obtained as a result of one-step gradient method ( $m_1$ =0,  $m_2$ =0). Increasing the steps number led to reduced average percentage prediction error. The error minimum equal to 3.154 % was obtained for the parameters:  $m_1$ =2,  $m_2$ =2,  $\alpha$ =0.5,  $\alpha$ =0.3,  $\alpha$ =0.2,  $\beta$ 0=5,  $\beta$ 1=3,  $\beta$ 2=2,  $\eta$ 0(0)= $\eta$ 1(0)== $\eta$ 2(0)=0.1.

Similar results were obtained in other simulations. It can be stated that the implementation of the multi-step technique enables higher accuracy of prediction by reduction of error  $J_P$ .

### 6. Conclusion

This paper contains description of FCM and multi-step supervised learning based on gradient method and real data. Simulation analysis of FCM and multi-step algorithms was realized in ISEMK on the example of prediction of individual household electric power consumption. Learned system was tested from the point of view of prediction accuracy for 100 test records. Chosen results of simulations, that show sufficient effectiveness of modeling based on FCM, were presented. The advantage of the application of the multi-step technique is improvement of the operation of the analyzed system by reduction of prediction error. Moreover, there are plans of further development of multi-step algorithms, as possible generalization of known one-step methods of learning.

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# Analiza rozmytych map kognitywnych w predykcji zużycia energii elektrycznej przez gospodarstwo domowe

Streszczenie: Praca poświęcona jest analizie symulacyjnej zastosowania rozmytej mapy kognitywnej (FCM) w predykcji zużycia energii elektrycznej przez gospodarstwo domowe. Opisano rozmyte mapy kognitywne oraz wielokrokowe uczenie nadzorowane oparte na metodzie gradientowej i rzeczywistych danych. Przy pomocy opracowanego środowiska ISEMK (inteligentny system ekspertowy oparty na mapach kognitywnych) zaimplementowano model systemu predykcji zużycia energii elektrycznej przez gospodarstwo domowe. Przeprowadzono badania symulacyjne wielokrokowego uczenia oraz testowania działania rozmytej mapy kognitywnej na podstawie rzeczywistych danych. Przedstawiono wybrane wyniki symulacji.

**Słowa kluczowe:** rozmyte mapy kognitywne, system predykcji, wielokrokowe uczenie nadzorowane, metoda gradientowa

### Prof. Aleksander Jastriebow, DSc

Prof. Aleksander Jastriebow, DSc, is Professor at Dept. of Computer Science Applications at the Kielce University of Technology and the Kazimierz Pulaski University of Technology and Humanities in Radom. He is a specialist in the field of mathematics and applied informatics. He is author and coauthor of more than 250 scientific papers. His



research interests include automation, informatics, diagnostics and artificial intelligence.

e-mail: a.jastriebow@tu.kielce.pl

### Katarzyna Piotrowska, MSc

Katarzyna Piotrowska is assistant at Dept. of Computer Science Applications at the Kielce University of Technology. She is author and coauthor of 8 scientific papers. Her research interests include expert systems, fuzzy cognitive maps, machine learning and decision support systems.



e-mail: k.piotrowska@tu.kielce.pl